



# Testing Standard Model and New Physics with the Unitarity Triangle fit

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on behalf of **UT<sub>fit</sub>** Collaboration

<http://www.utfit.org>

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# Unitarity Triangle

Using the Unitarity of the CKM matrix in the SM we can build the Unitarity Triangle.

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

CP violation in SM is ruled only by one parameter.

- Determine it in several ways (test of SM)
- Fit simultaneously for SM and

**UT<sub>fit</sub> Coll,**  
[hep-ph/0501199](https://arxiv.org/abs/hep-ph/0501199)

**UT<sub>fit</sub> Coll,**  
[hep-ph/0509219](https://arxiv.org/abs/hep-ph/0509219)

New Physics quantities

$$\alpha = \pi - \beta - \gamma$$

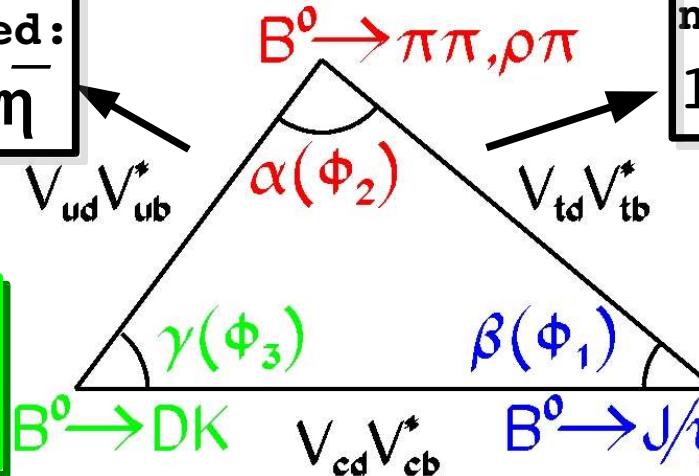
normalized:  
 $\bar{\rho} + i \bar{\eta}$

$$V_{ud}V_{ub}^*$$

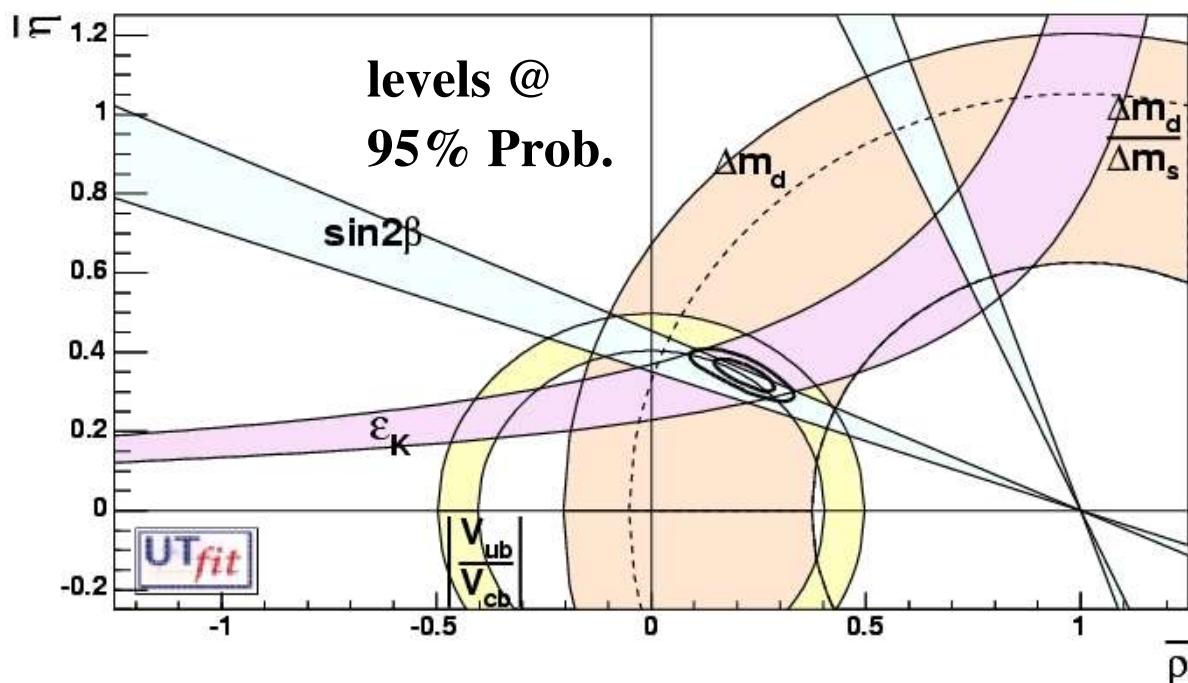
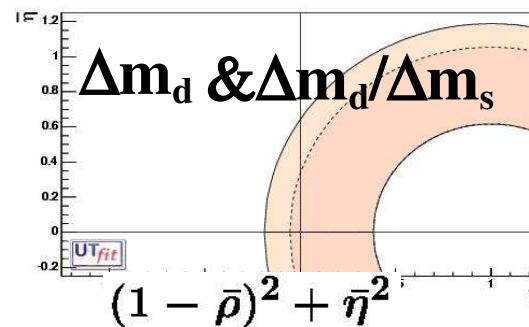
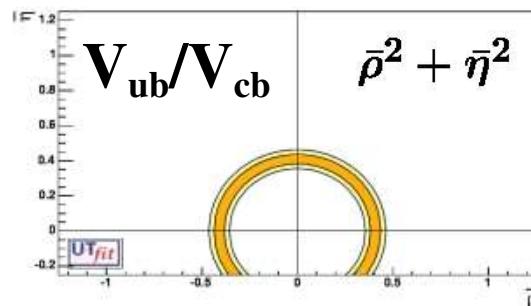
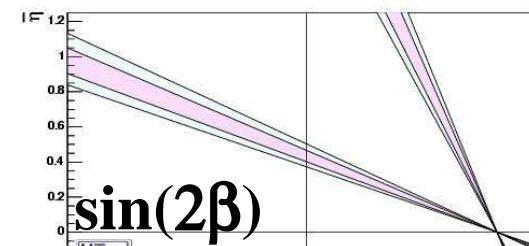
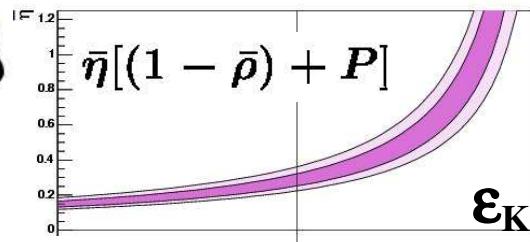
normalized:  
 $1 - \bar{\rho} + i \bar{\eta}$

$$\beta = \text{atan} \left( \frac{\bar{\eta}}{(1 - \bar{\rho})} \right)$$

$$\gamma = \text{atan} \left( \frac{\bar{\eta}}{\bar{\rho}} \right)$$



# The “Classic Fit”...



$$\bar{\rho} = 0.214 \pm 0.047$$

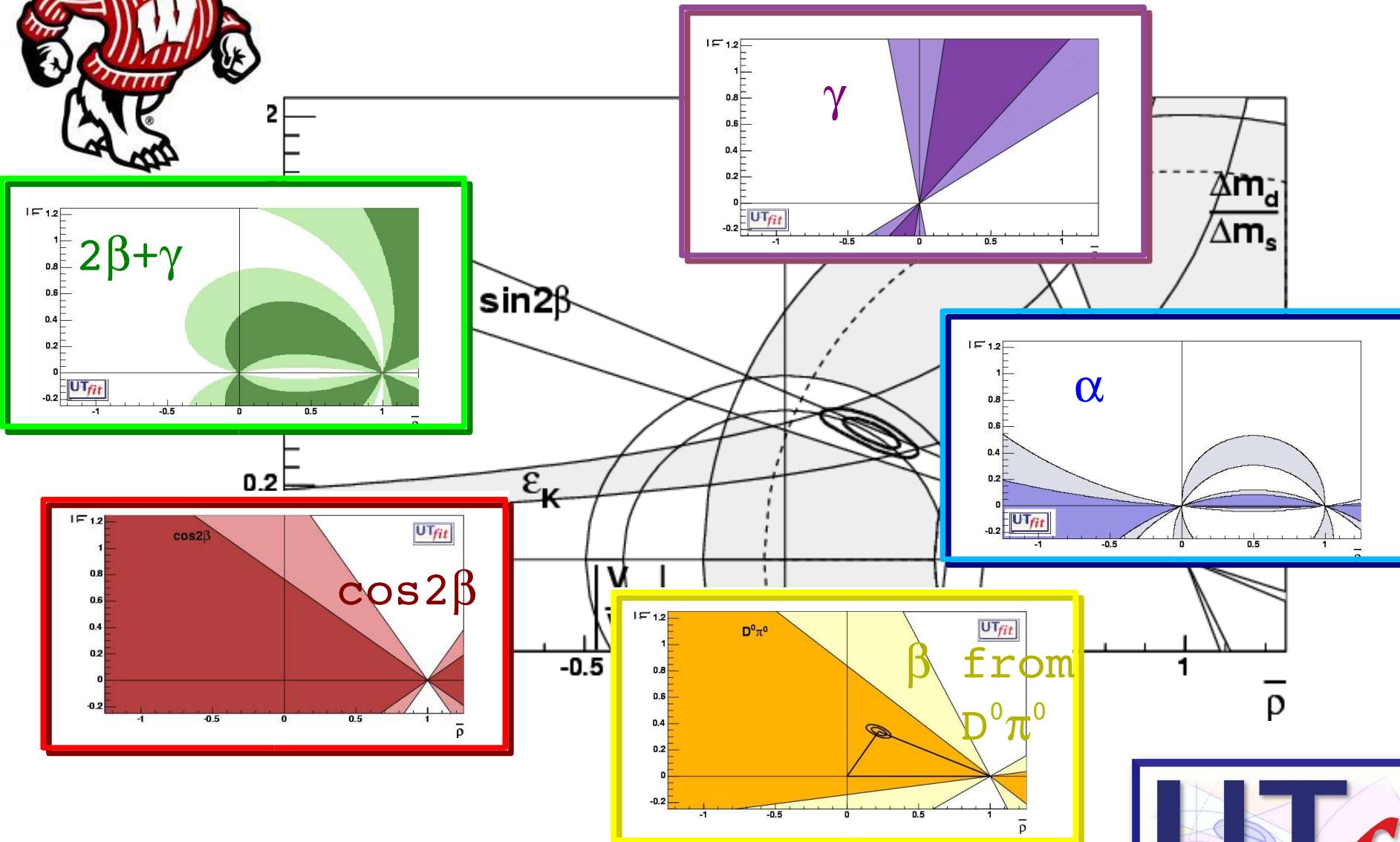
$[0.112, 0.307]$  @ 95% Prob.

$$\bar{\eta} = 0.343 \pm 0.028$$

$[0.289, 0.396]$  @ 95% Prob.



# ..and new bounds from B factories





# $\alpha$ from isospin analysis: $\pi\pi$ , $\rho\rho$ , $\rho\pi$

See J.Malclès' &  
A.Kusaka's talks

From the SU(2)  
amplitudes ( $\pi\pi$ ,  $\rho\rho$ ):

$$A^{+-} = -Te^{-i\alpha} + Pe^{i\delta P}$$

$$A^{+0} = -1/\sqrt{2} e^{-i\alpha} (T + T_C e^{i\delta C})$$

$$A^{00} = -1/\sqrt{2} (T_C e^{i\delta C} e^{-i\alpha} + Pe^{i\delta P})$$

unknowns:  $T$ ,  $P$ ,  $T_C$ ,  $\delta_P$ ,  $\delta_{T_C}$ ,  $\alpha$

observable: 3x BR,  $C_{+-}$ ,  $S_{+-}$ ,  $C_{00}$

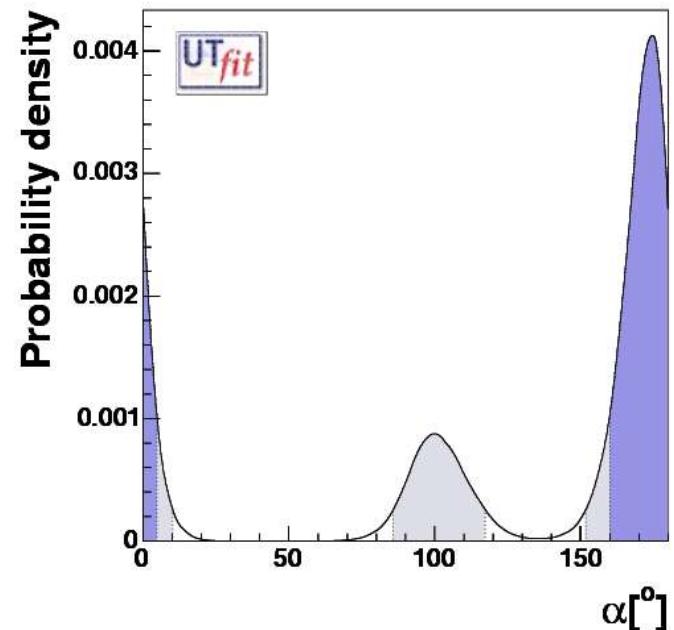
Similar analysis for  $(\rho\pi)^0$  on the Dalitz plane

$$A^k = T^k e^{-i\alpha} + P^k$$

$$\bar{A}^k = T^{\bar{k}} e^{i\alpha} + P^{\bar{k}}$$

with

$k=+-$  for  $\rho^+\pi^-$ ,  $-+$  for  $\rho^-\pi^+$ ,  
 $\epsilon 00$  for  $\rho^0\pi^0$

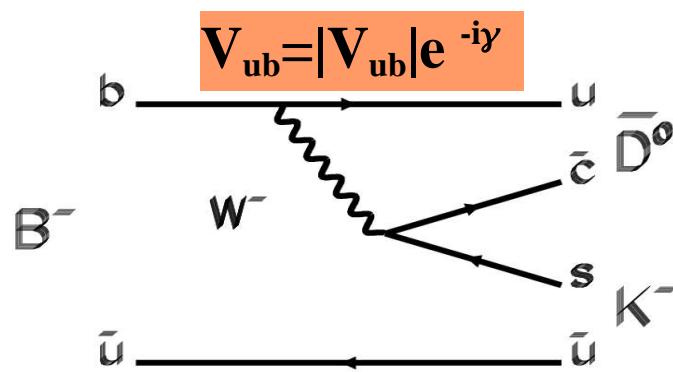


$\alpha = [86, 107]^\circ \cup [152, 90]^\circ$   
@ 95% Prob.

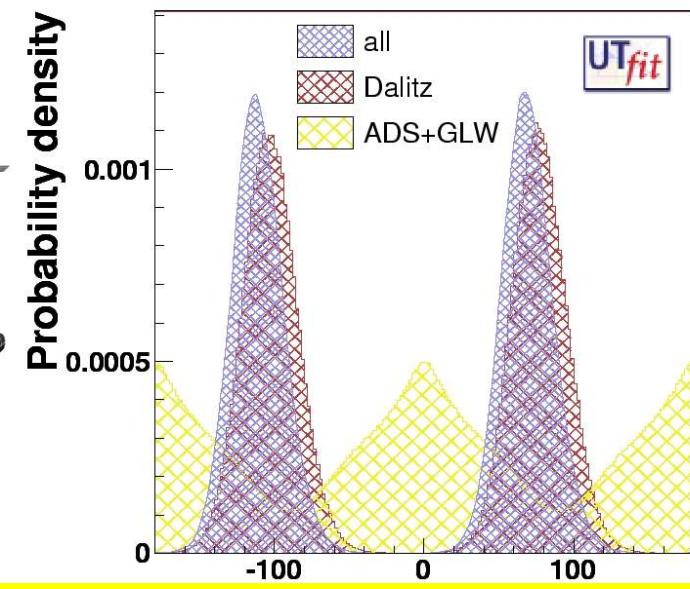
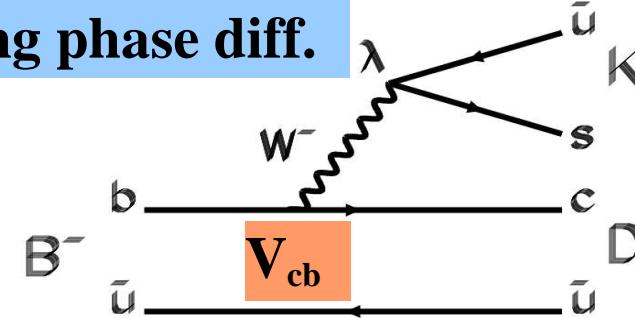


# $\gamma$ from $B \rightarrow D^{(*)} K^{(*)}$ decays

$r_B$  = ratio of amplitudes  
 $\delta_B$  = strong phase diff.



See J. Malclès' talk



$$\gamma = (66 \pm 17)^\circ \text{ U } (-114 \pm 187)^\circ$$

- ADS (Atwood, Dunietz, Soni) method:

$B^0$  and  $\bar{B}^0$  into the same final state

$$R_{ADS} = r_B^2 + r_{DCS}^2 + 2r_B r_{DCS} \cos \gamma \cos(\delta_B + \delta_D)$$

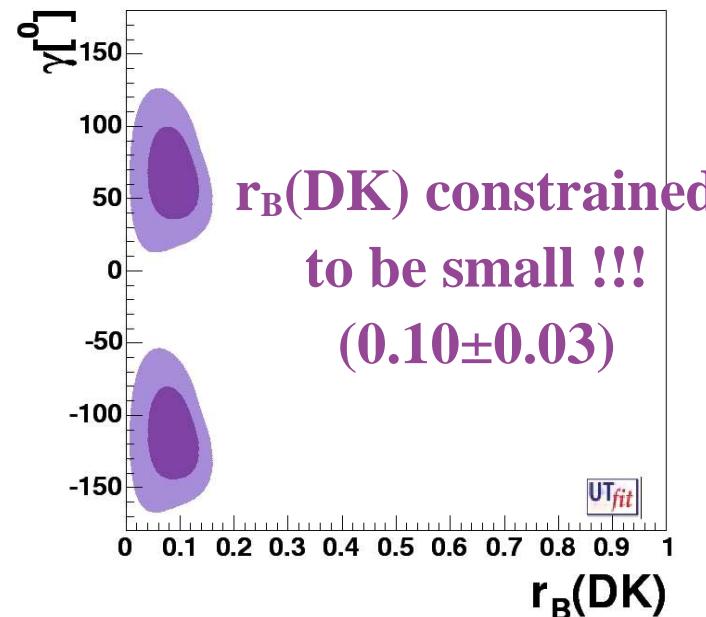
- GLW (Gronau, Londow, Wyler) method:

use the CP eigenstates  $D^{(*)0}_{CP}$

$$R_{CP\pm} = 1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B$$

- D<sup>0</sup> Dalitz plot analysis with

$$B^- \rightarrow D^{(*)0} [K_S \pi^+ \pi^-] K^-$$



$r_B(DK)$  constrained to be small !!!  
 $(0.10 \pm 0.03)$

UTfit

UTfit

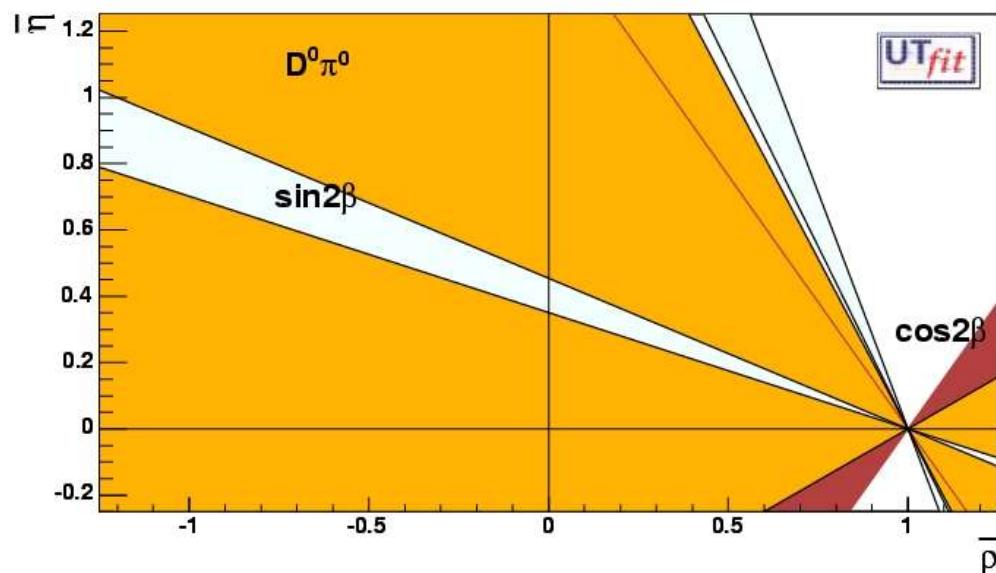
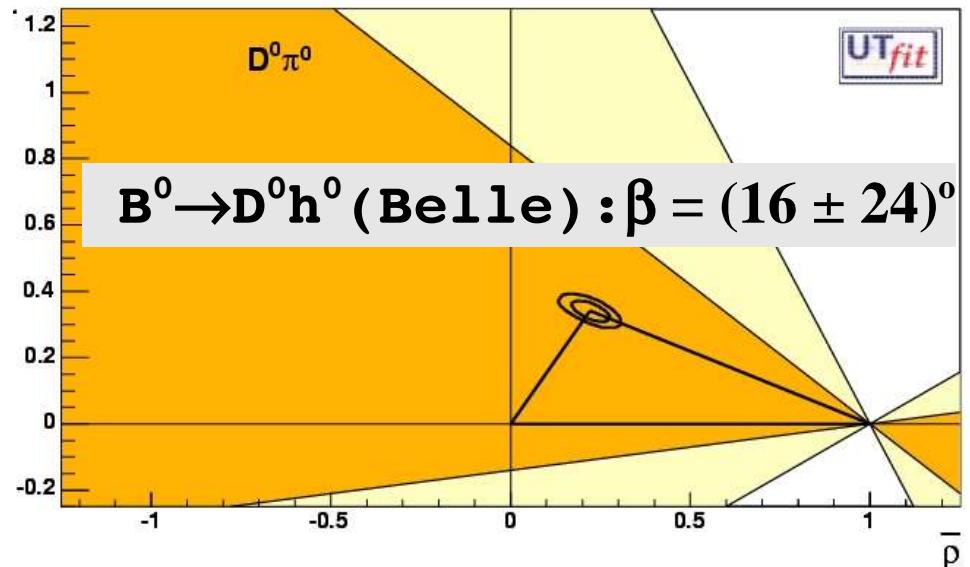
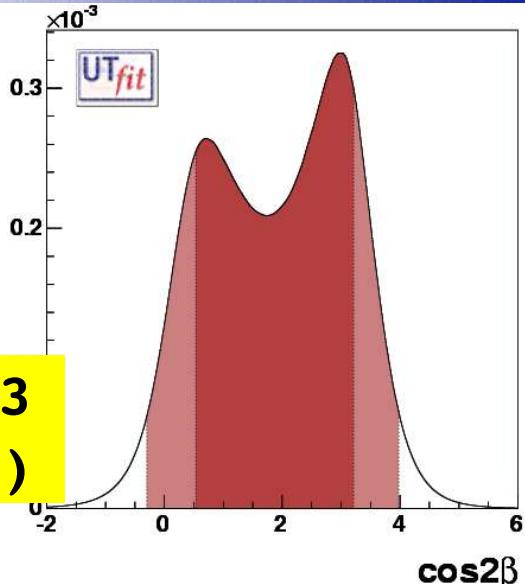
$r_B(DK)$



# $\cos 2\beta$ from $B \rightarrow J/\psi K^{*0}$ and $B \rightarrow D^0 h^0$

$\cos 2\beta = 1.9 \pm 1.3$   
(BaBar+Belle)

Probability density



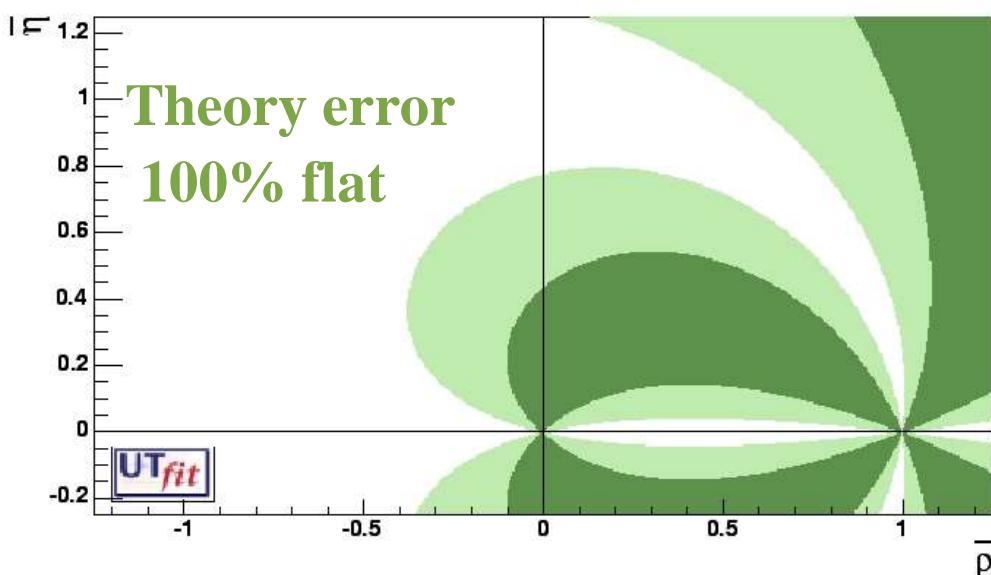
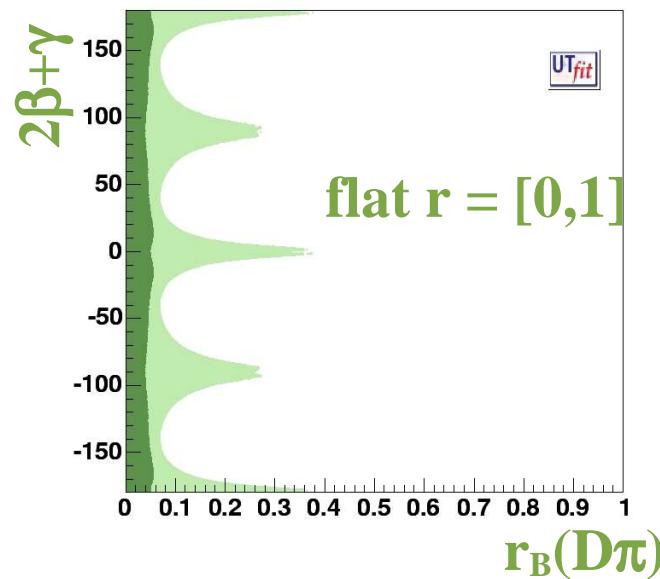
Removes the ambiguity on  
 $\beta$  coming from  $\sin 2\beta$



# 2 $\beta$ + $\gamma$ from $B \rightarrow D^{(*)}\pi(\rho)$

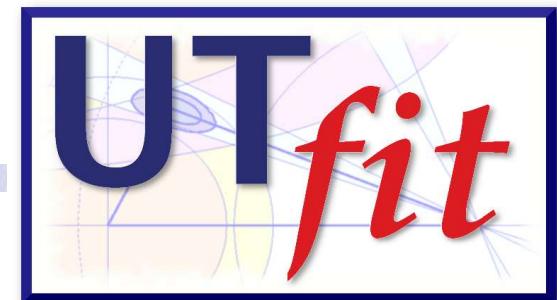
$$a^{(*)} = 2r^{(*)}\sin(2\beta+\gamma)\cos\delta^{(*)}$$

$$c_{\text{lep}}^{(*)} = 2r^{(*)}\cos(2\beta+\gamma)\sin\delta^{(*)}$$



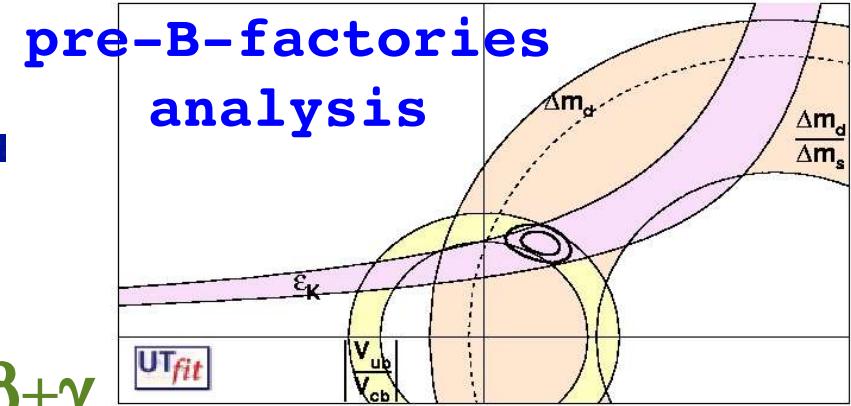
- ✚ Interference  $b \rightarrow u$  vs  $b \rightarrow c$  like in DK decays
- ✚ Open system: 2 observables for  $2\beta+\gamma$ ,  $r$  and  $\delta$
- ✚ Only assuming  $r$  we can extract  $2\beta+\gamma$ 
  - ◆ Extraction of  $r$  from  $B \rightarrow D_s\pi$
  - ◆ Theory error ~100% flat to take into account SU(3) breaking and annihilations in  $B \rightarrow D\pi$

See D. Pirjol, talk at  
Beauty 2005

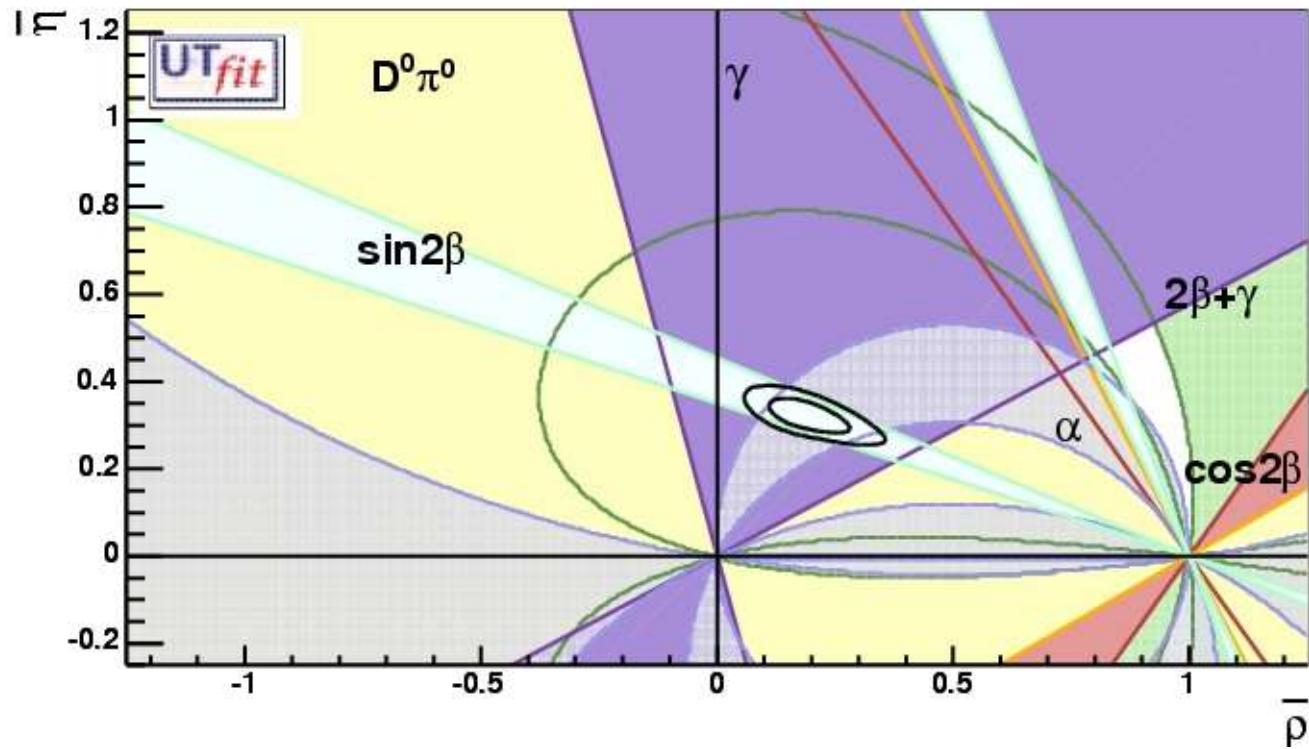




# Angles Only



$$\sin 2\beta + \cos 2\beta + \beta + \gamma + \alpha + 2\beta + \gamma$$



Precision  
comparable to the  
pre-B-factories  
analysis

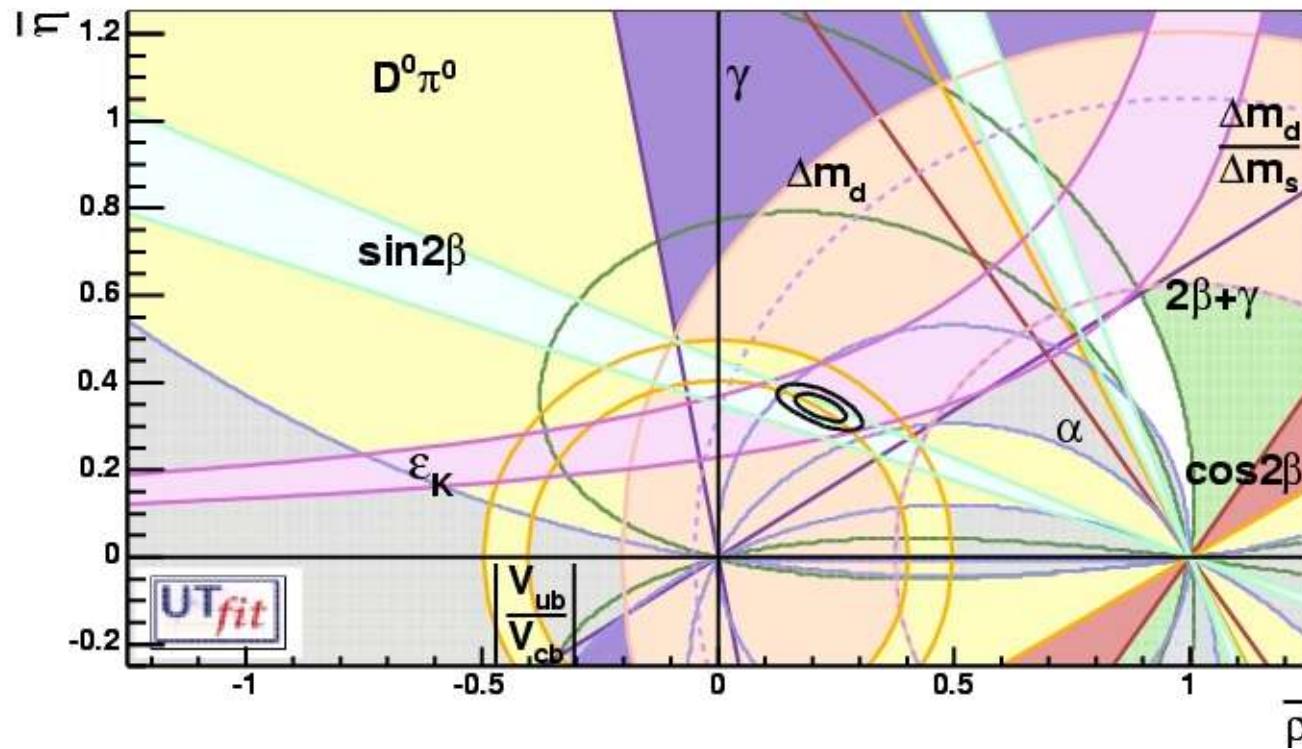
$\bar{\rho} = 0.193 \pm 0.057$   
 $[0.083, 0.321] @ 95\% \text{ Prob.}$

$\bar{\eta} = 0.321 \pm 0.027$   
 $[0.266, 0.376] @ 95\% \text{ Prob.}$



# Including all the constraints

classic fit +  $\cos 2\beta$  +  $\beta$  +  $\gamma$  +  $\alpha$  +  $2\beta + \gamma$



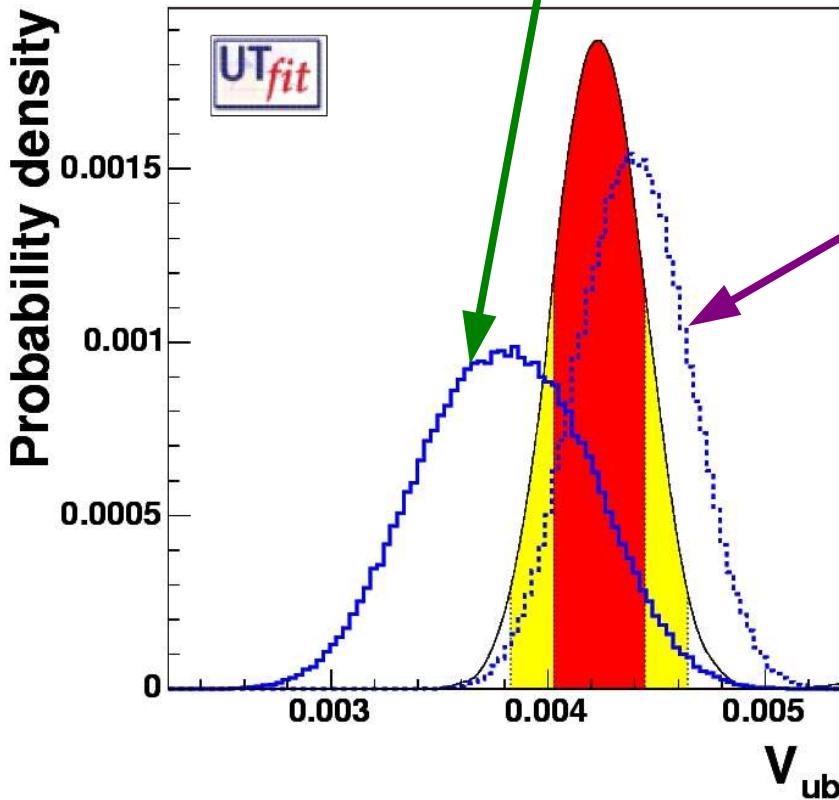
$\bar{\rho} = 0.216 \pm 0.036$   
[0.143, 0.288] @ 95% Prob.

$\bar{\eta} = 0.342 \pm 0.022$   
[0.300, 0.385] @ 95% Prob.



# Tension in the fit

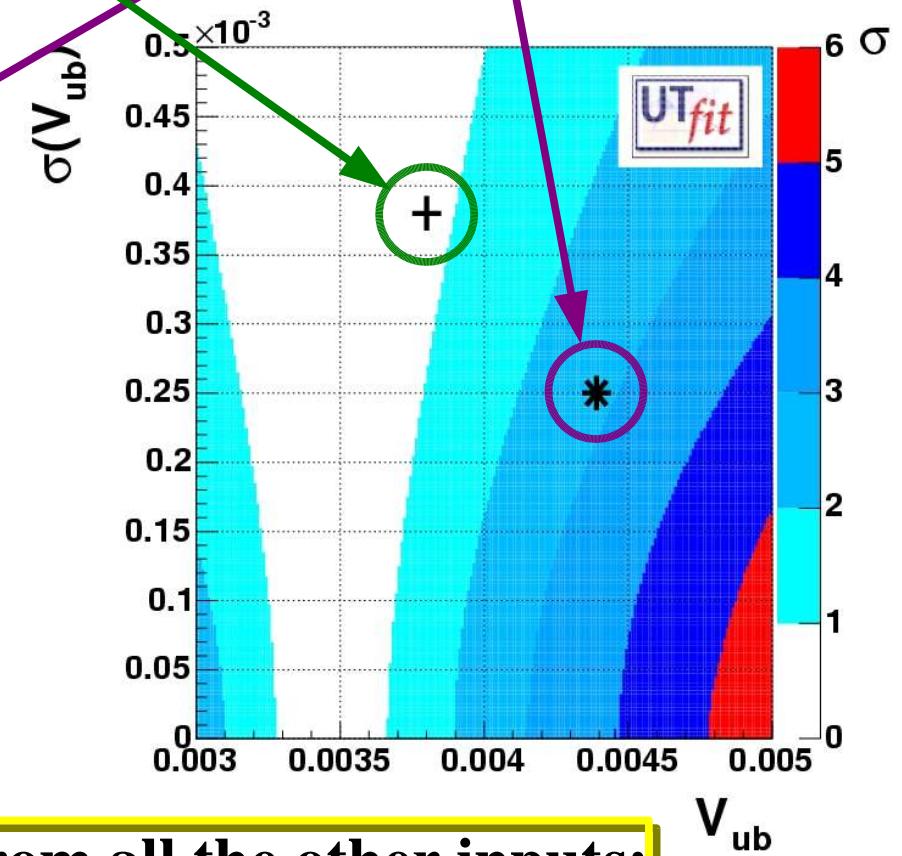
exclusive: BRs from HFAG;  
form factor from  
quenched LQCD  
 $V_{ub} = (3.80 \pm 0.27 \pm 0.47) 10^{-3}$



incl.+excl.

$$V_{ub} = (4.22 \pm 0.20) 10^{-3}$$

inclusive from HFAG  
 $V_{ub} = (4.38 \pm 0.19 \pm 0.27) 10^{-3}$



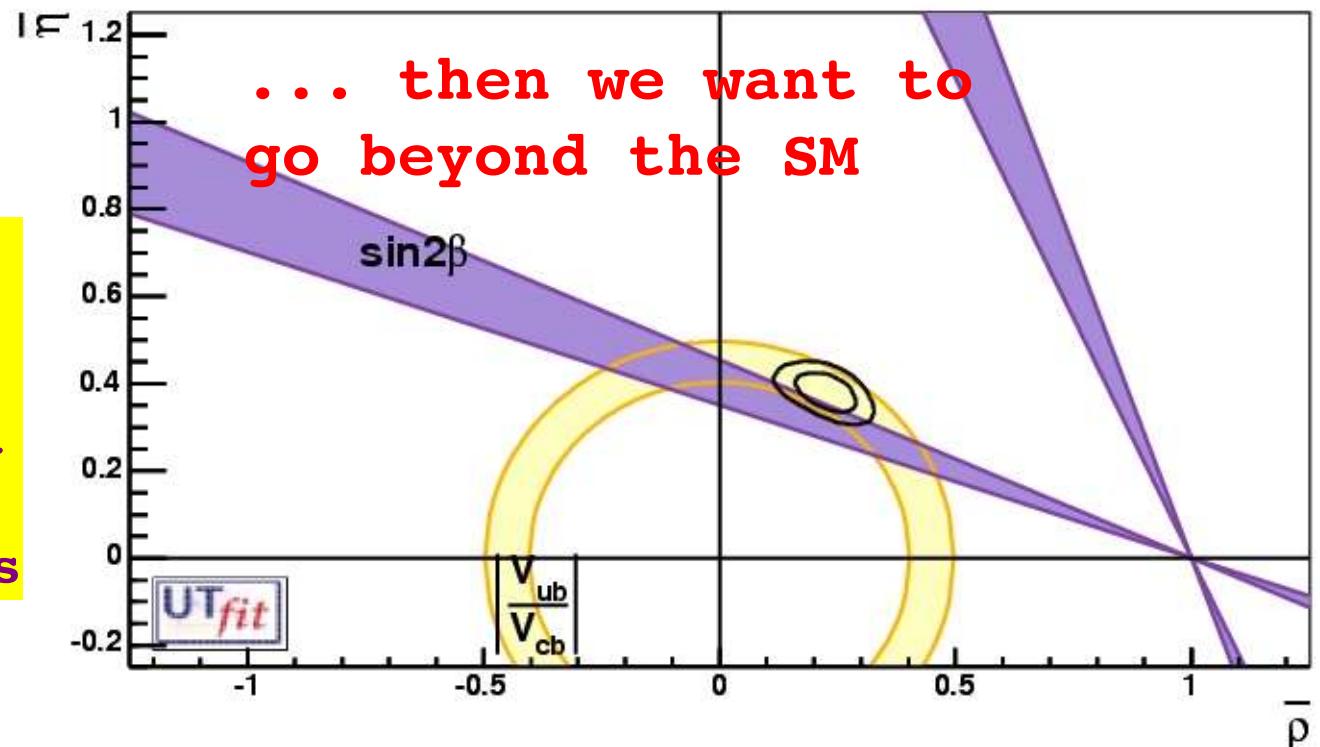
from all the other inputs:

$$V_{ub} = (3.48 \pm 0.20) 10^{-3}$$



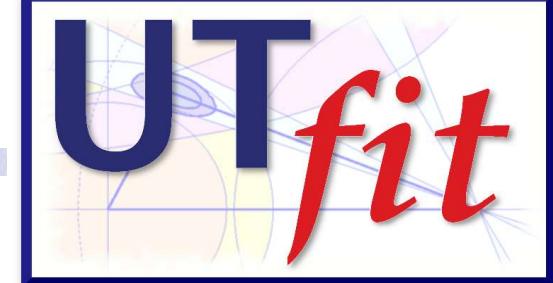
# But if you believe into $V_{ub}$ ...

Ciuchini, M.P.,  
Silvestrini  
hep-ph/0507290  
Model independent  
estimation of  
theoretical errors



$\sin 2\beta = 0.791 \pm 0.034$   
from indirect determination

$\sin 2\beta = 0.687 \pm 0.032 \pm 0.017$   
From direct measurement





# Fit with NP-independent constraints

Assuming no NP at tree level

the effect of the  $D^0$ - $\bar{D}^0$  mixing to  $\gamma$

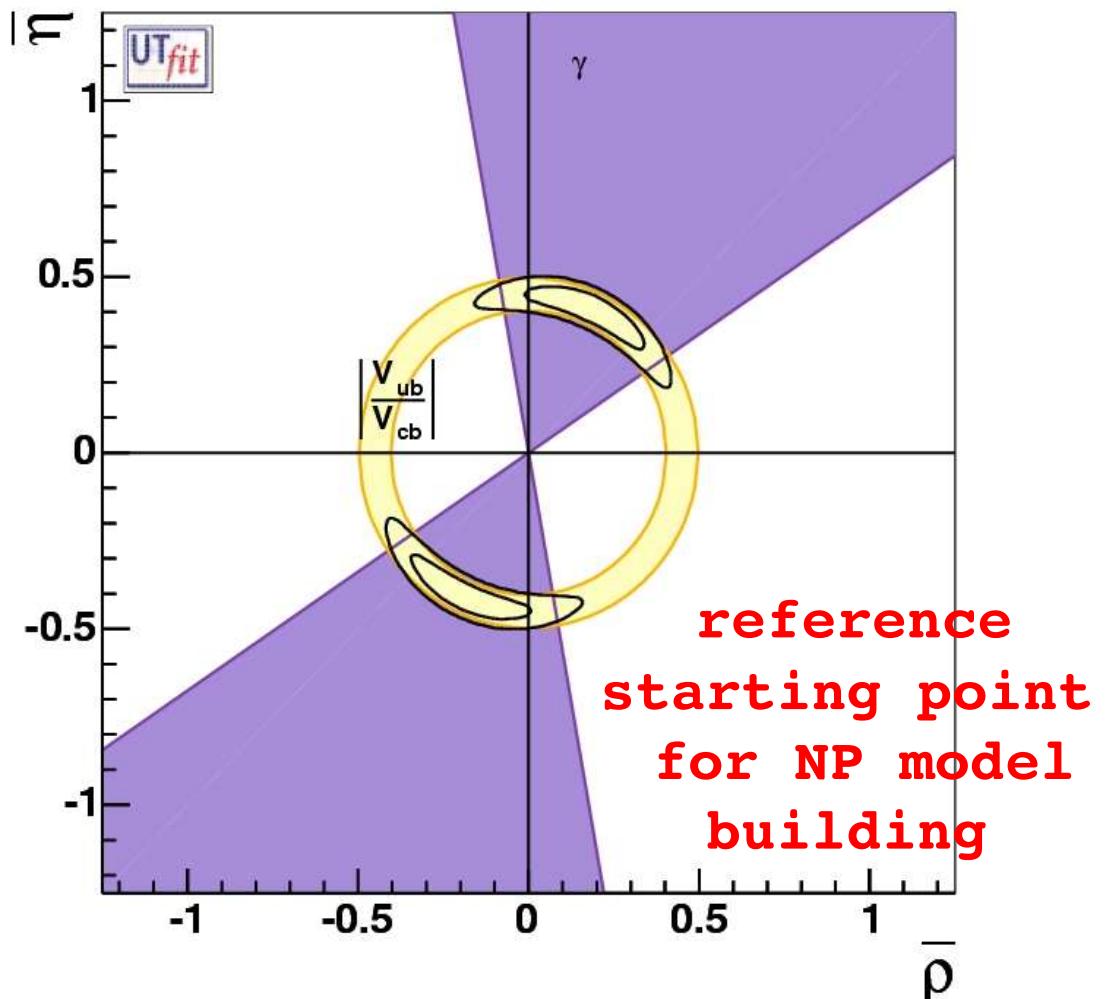
is negligible wrt the actual error

semileptonic decays are clean

We have a NP free determination of  $\bar{\rho}$  and  $\bar{\eta}$

$$\bar{\rho} = \pm 0.18 \pm 0.11$$

$$\bar{\eta} = \pm 0.41 \pm 0.05$$





# NP: model independent approach

We can generalize the analysis beyond the Standard Model parameterizing the deviations in  $|\Delta F|=2$  processes in a model independent way:

- $|\varepsilon_K|^{\text{EXP}} = C_\varepsilon \cdot |\varepsilon_K|^{\text{SM}}$
  - $\Delta m_s^{\text{EXP}} = C_s \cdot \Delta m_s^{\text{SM}}$
  - $\alpha^{\text{EXP}} = \alpha^{\text{SM}} - \phi_{\text{Bd}}$
  - $\Delta m_d^{\text{EXP}} = C_d \cdot \Delta m_d^{\text{SM}}$
  - $A_{\text{CP}}(\text{J}/\psi K^0) = \sin(2\beta + 2\phi_{\text{Bd}})$
- 5 unknowns

	$\rho, \eta$	$C_d, \phi_d$	$C_{\varepsilon K}$	$C_s, \phi_s$
$V_{ub}/V_{cb}$	X			
$\Delta m_d$	X	X		
$\varepsilon_K$	X		X	
$A_{\text{CP}}(\text{J}/\psi K)$	X	X		
$\alpha(\rho\rho, \rho\pi, \pi\pi)$	X	X		
$\gamma(DK)$	X			
$\Delta m_s$				X
$A_{\text{CP}}(\text{J}/\psi \phi)$	~X	not yet available		X
$\gamma(D_s K)$	X			X

## model independent assumptions

- J. M. Soares and L. Wolfenstein, Phys. Rev. D 47 (1993) 1021;  
 N. G. Deshpande, B. Dutta and S. Oh, Phys. Rev. Lett. 77 (1996) 4499  
 [arXiv:hep-ph/9608231]
- J. P. Silva and L. Wolfenstein, Phys. Rev. D 55 (1997) 5331 [arXiv:hep-ph/9610208]
- A. G. Cohen *et al.*, Phys. Rev. Lett. 78 (1997) 2300 [arXiv:hep-ph/9610252]
- Y. Grossman, Y. Nir and M. P. Worah, Phys. Rev. Lett. B 407 (1997) 307  
 [arXiv:hep-ph/9704287]

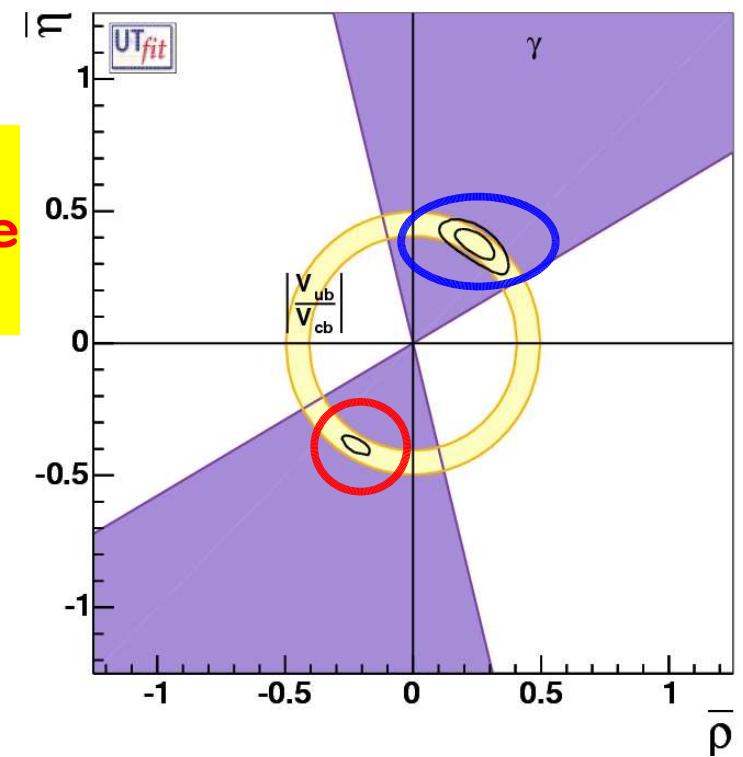
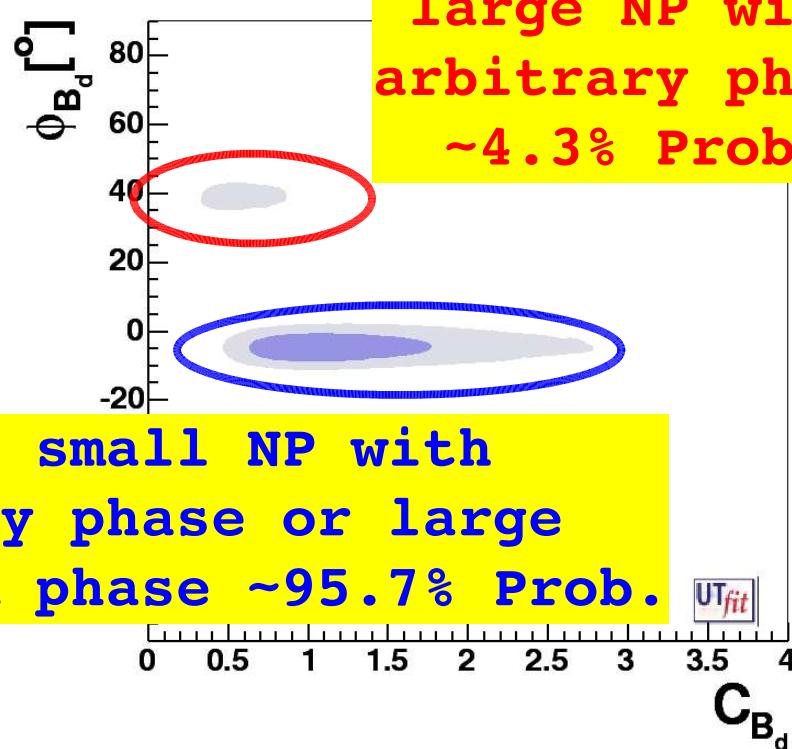


# The UT<sub>fit</sub> beyond the SM

"SM"  $\bar{\rho} = 0.246 \pm 0.053$

"NP" [-0.230, -0.212] @ 95% Prob.

"SM"  $\bar{\eta} = 0.379 \pm 0.039$   
 "NP" [-0.398, -0.381] @ 95% Prob.





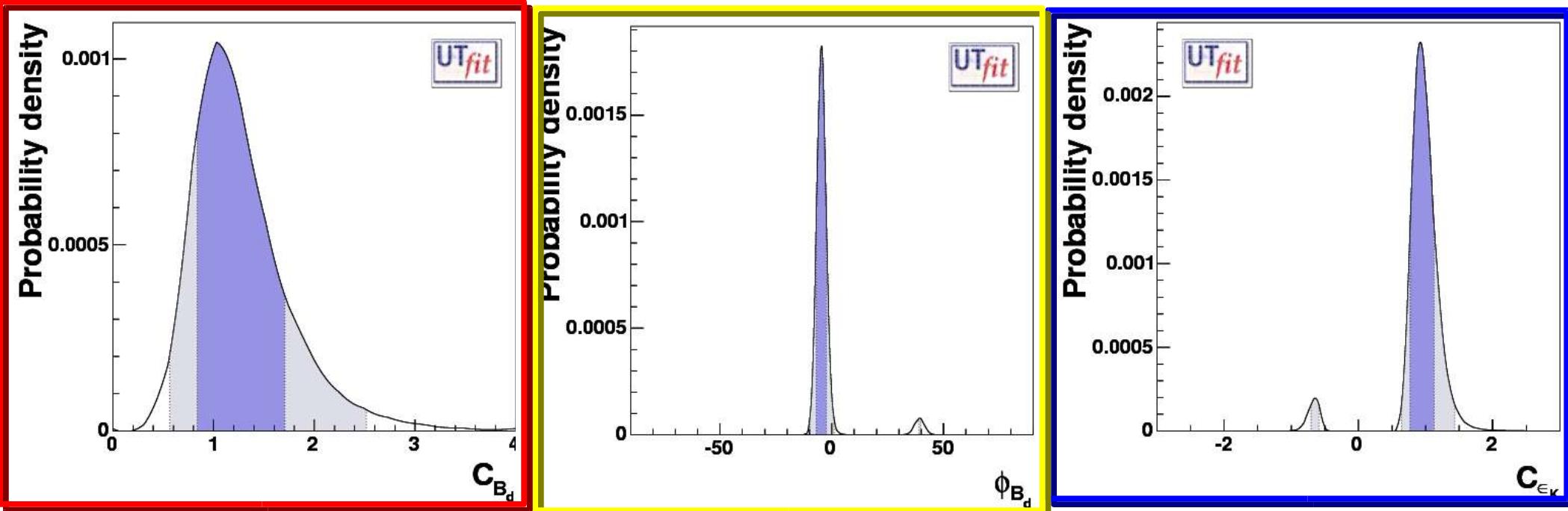
# Bounds on NP parameters

NP in  $\Delta B=2$  and  $\Delta S=2$  could be up to 50% with respect to the SM only if it has the same phase of the SM

$$C_{B_d} = 1.27 \pm 0.44$$

$$\phi_{B_d} = -4.7 \pm 2.3^\circ$$

$$C_{\varepsilon_K} = 0.95 \pm 0.18$$

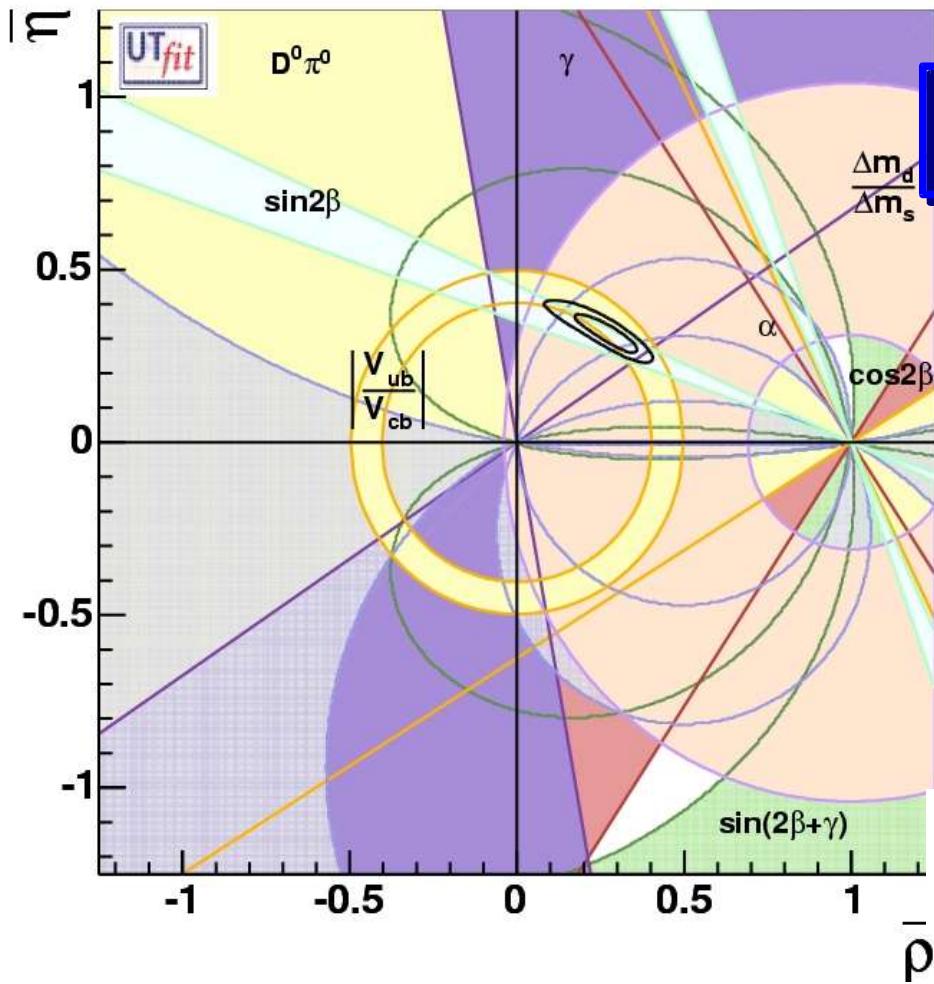




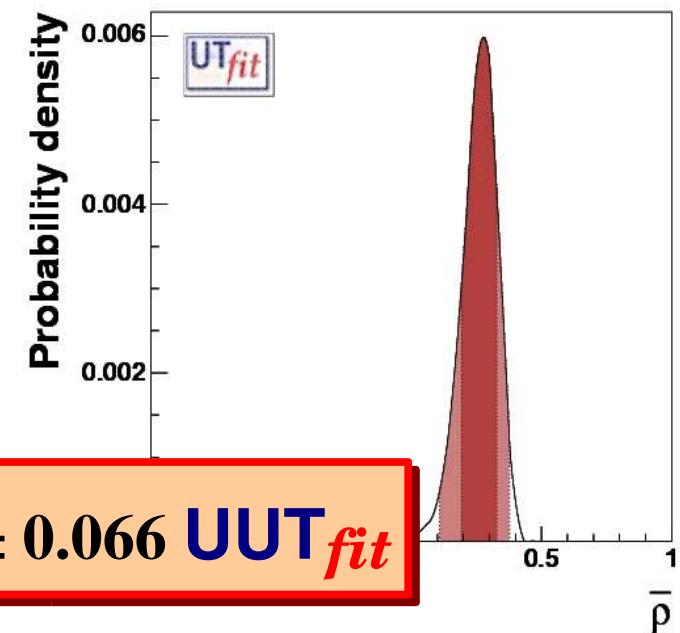
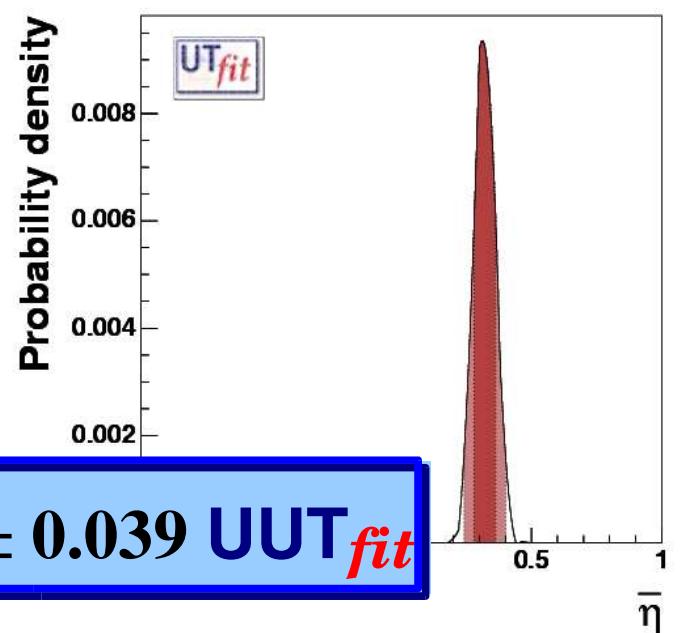
# Universal UT $\textit{fit}$ : reference for SM and MFV

Buras et al.  
hep-ph/0007085

MFV = CKM is the only source  
of flavour mixing.  $\varepsilon_K$  and  $\Delta m_d$  are not  
used (sensitive to NP).



$$\bar{\eta} = 0.319 \pm 0.039 \text{ UUT}\textit{fit}$$



$$\bar{\rho} = 0.258 \pm 0.066 \text{ UUT}\textit{fit}$$



## Bounds on NP in MFV from UUT<sub>fit</sub>: Small tan $\beta$

NP enters as additional contribution to the top box diagram

D'Ambrosio et al.  
hep-ph/0207036

$$S_0(x_t) \rightarrow S_0(x_t) + \delta S_0(x_t)$$

$$\delta S_0(x_t) = 4a \left( \frac{\Lambda_0}{\Lambda} \right)^2$$

a = 1 (as a reference)

$$\Lambda_0 = 2.4 \text{ TeV}$$

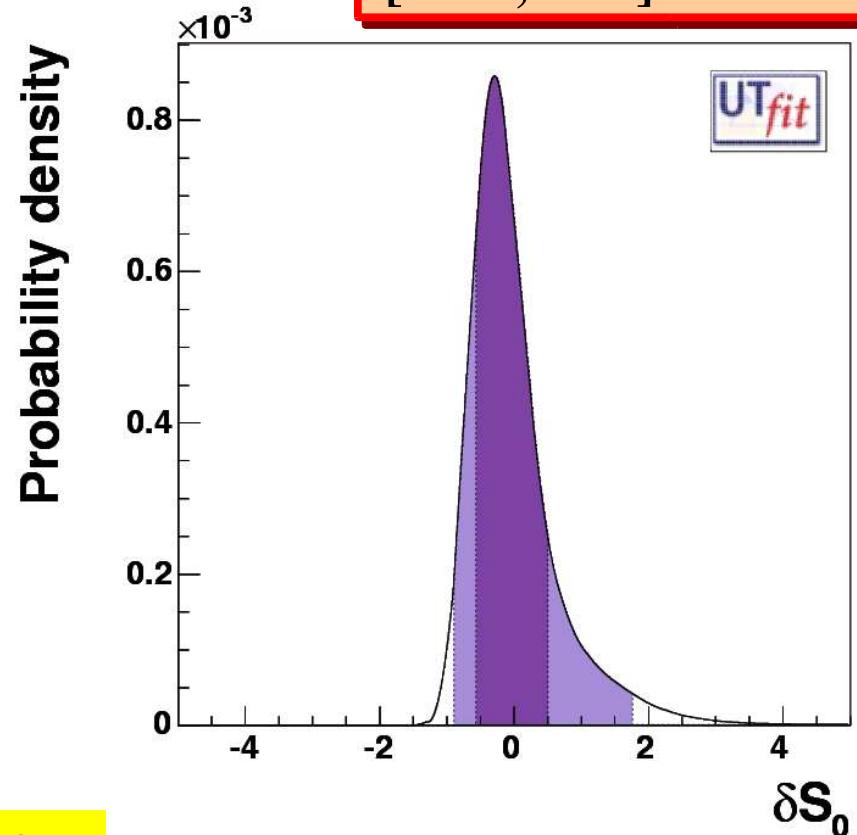
$\Lambda_0$  is the equivalent SM scale

$\Lambda > 3.6 \text{ TeV} @ 95\%$  for  $\delta S_0(x_t) > 0$

$\Lambda > 5.1 \text{ TeV} @ 95\%$  for  $\delta S_0(x_t) < 0$

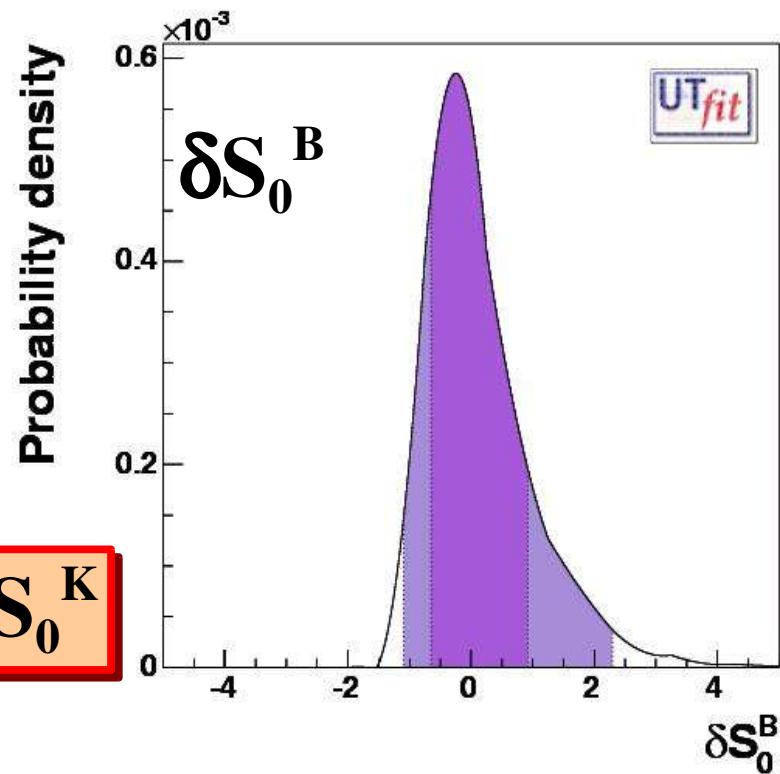
$$\delta S_0 = -0.03 \pm 0.54$$

[-0.90, 1.79] @ 95% Prob.

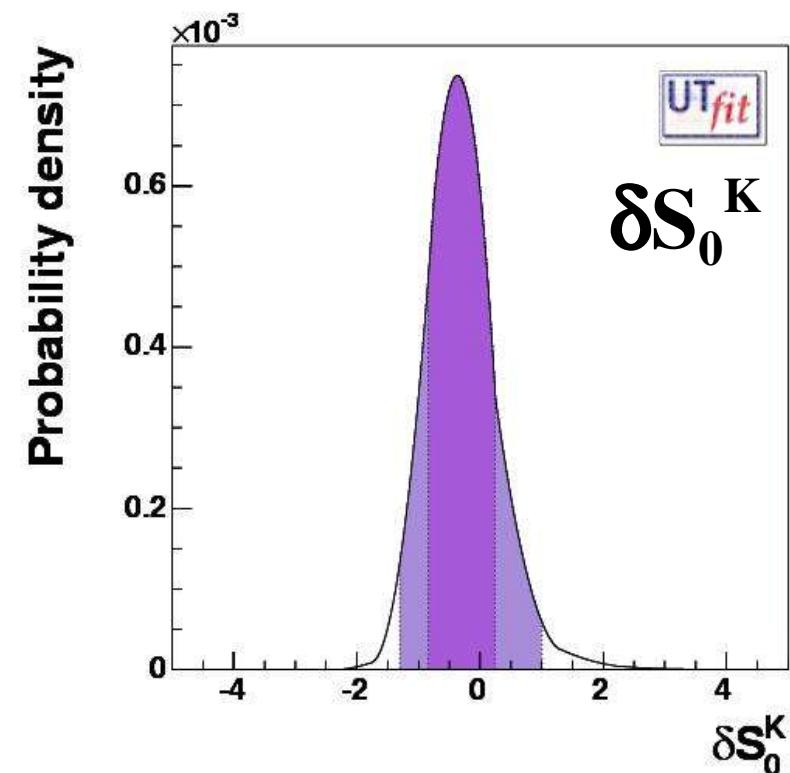




## Bounds on NP in MFV from UUT<sub>fit</sub>: Large tan $\beta$



$\delta S_0^B \neq \delta S_0^K$



$\Lambda > 2.6 \text{ TeV} @ 95\% \text{ for } \delta S_0(x_t) > 0$

$\Lambda > 4.9 \text{ TeV} @ 95\% \text{ for } \delta S_0(x_t) < 0$

$\Lambda > 3.2 \text{ TeV} @ 95\% \text{ for } \delta S_0(x_t) > 0$

$\Lambda > 4.9 \text{ TeV} @ 95\% \text{ for } \delta S_0(x_t) < 0$



# Conclusions

- + Large set of new bounds from B-factories allows overconstraining of the Unitarity Triangle
- + But the only tension in the fit comes from the "classic" constraints ( $\sin 2\beta$  vs  $V_{ub}$ )
- + We have a ("NP free") tree level determination of  $\bar{\rho}$  and  $\bar{\eta}$
- + All the NP models have to agree with it
- + We can start from here to fit SM ( $\bar{\rho}$  and  $\bar{\eta}$ ) and NP (corrections to SM in mixing and mixing phases) together
- + We go back to the SM solution (up to a fine tuned region)
- + Eighter NP effects are small with arbitrary phase...
- + ...Or NP effects are large with the same phase of SM MFV
  - ◆ UUT as the starting point of SM and MFV analysis
  - ◆ We can translate the measurement of MFV NP sensitive quantities (mixing) into bounds on tested scale



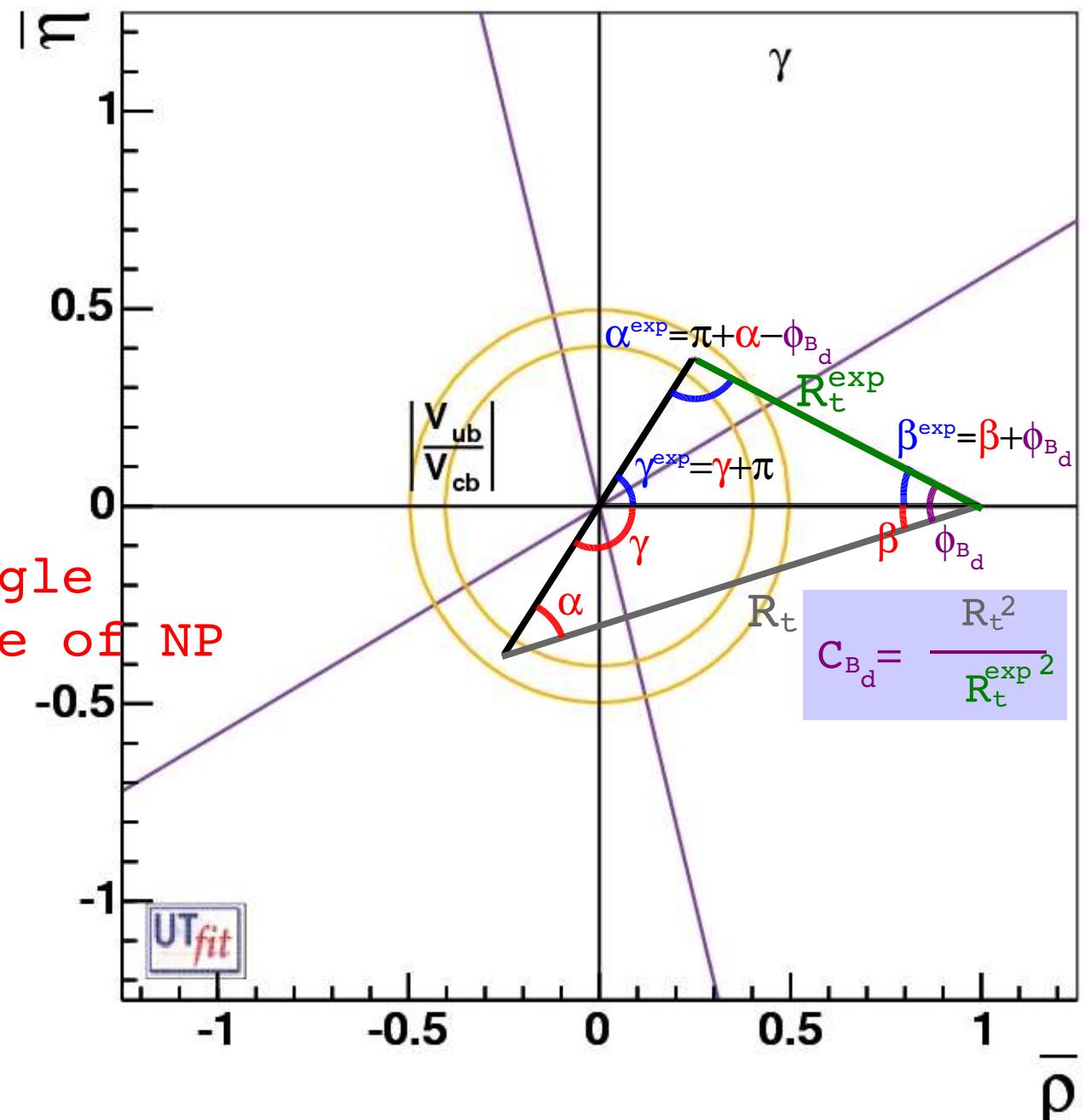
We need more data (a Super B factory?) to clarify the interesting situation



# Backup Slides

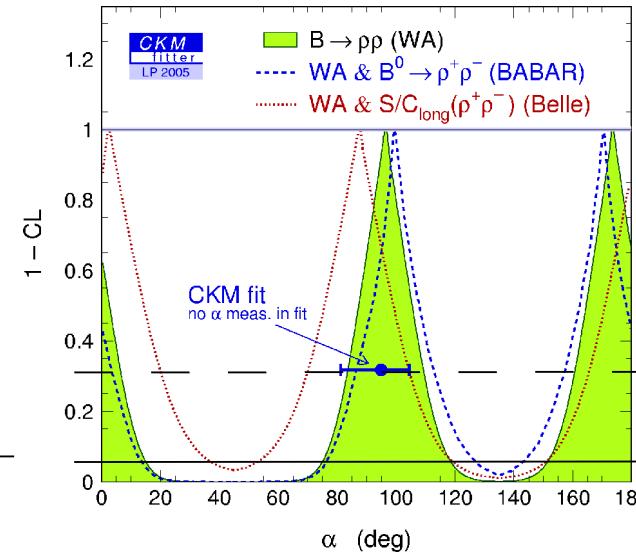
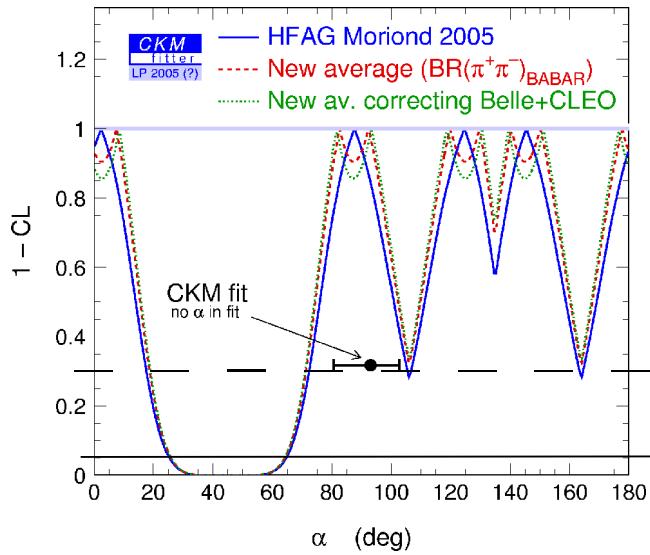
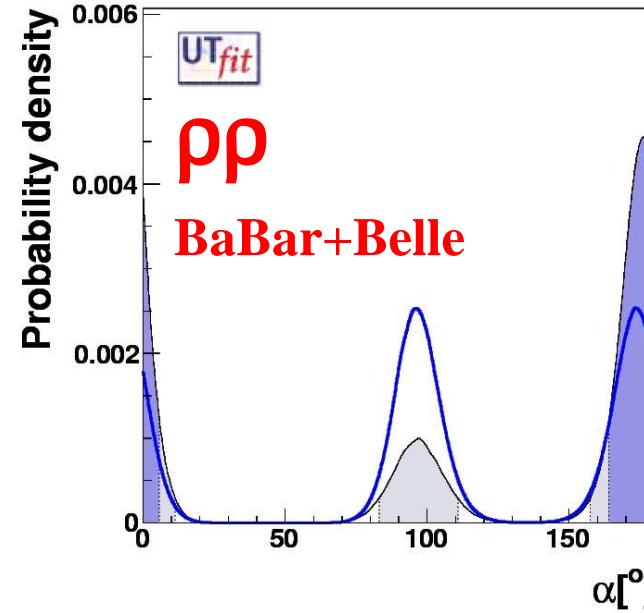
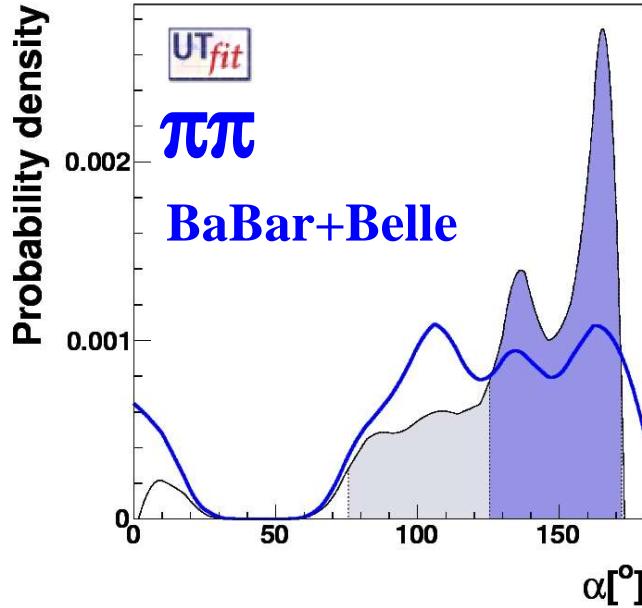


How the triangle  
change in the case of NP





# $\alpha$ from isospin analysis (III): $\pi\pi$ and $\rho\rho$



$C_{\pi\pi}$  and  $S_{\pi\pi}$  equal to 0  
are excluded

$$C_{\pi\pi} = -0.37 \pm 0.10$$
$$S_{\pi\pi} = -0.50 \pm 0.12$$

$$C_{\rho\rho} = -0.03 \pm 0.17$$
$$S_{\rho\rho} = -0.21 \pm 0.22$$

$C_{\rho\rho}$  and  $S_{\rho\rho}$  equal to 0  
are preferred





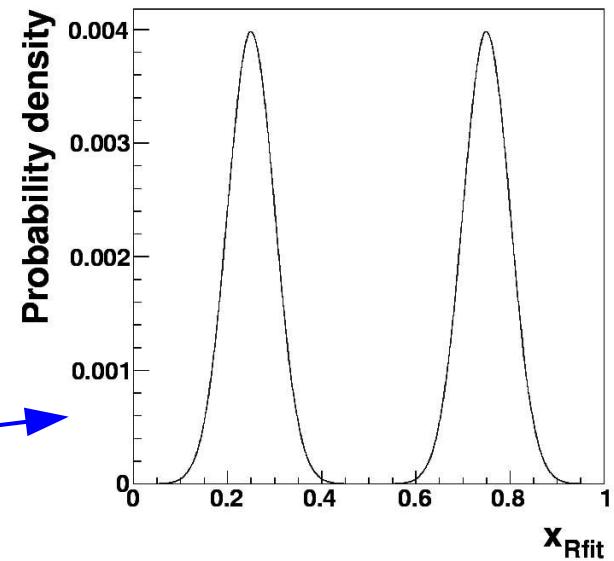
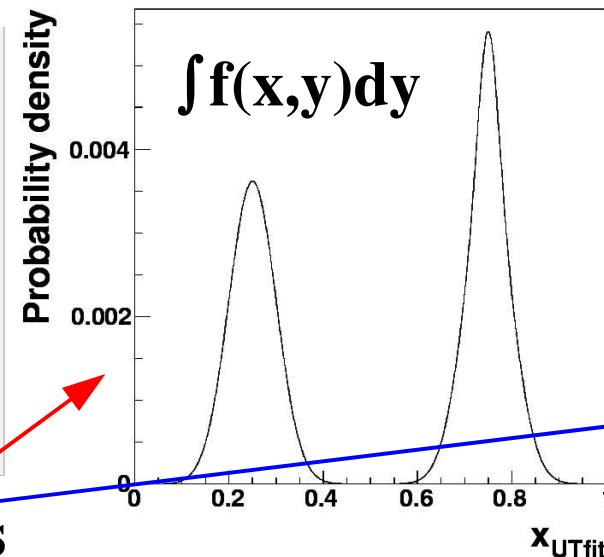
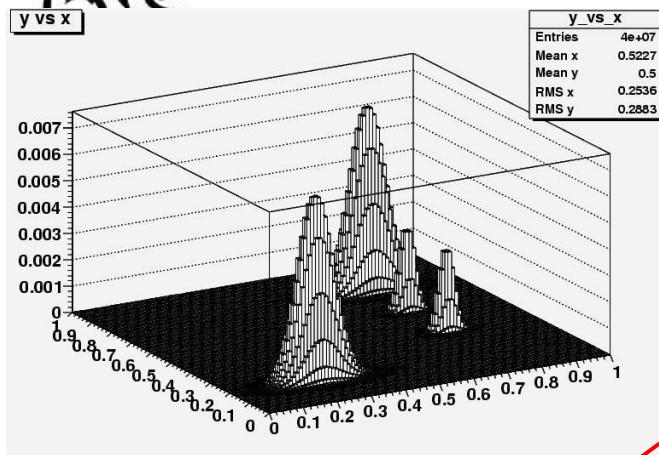
# $\alpha$ from isospin analysis (IV): toy

what does the difference  
in peak height mean?

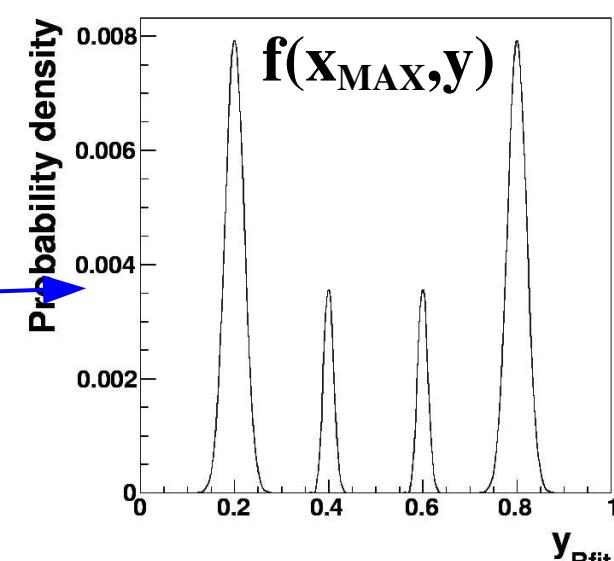
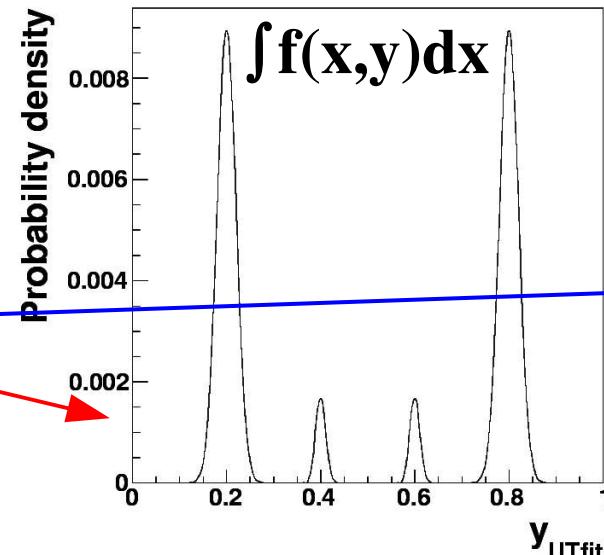
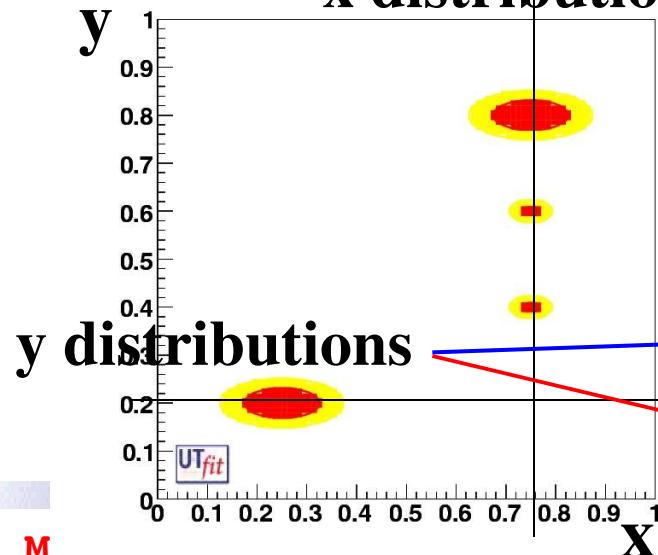
UTfit

Rfit

$f(x, y_{MAX})$



x distributions



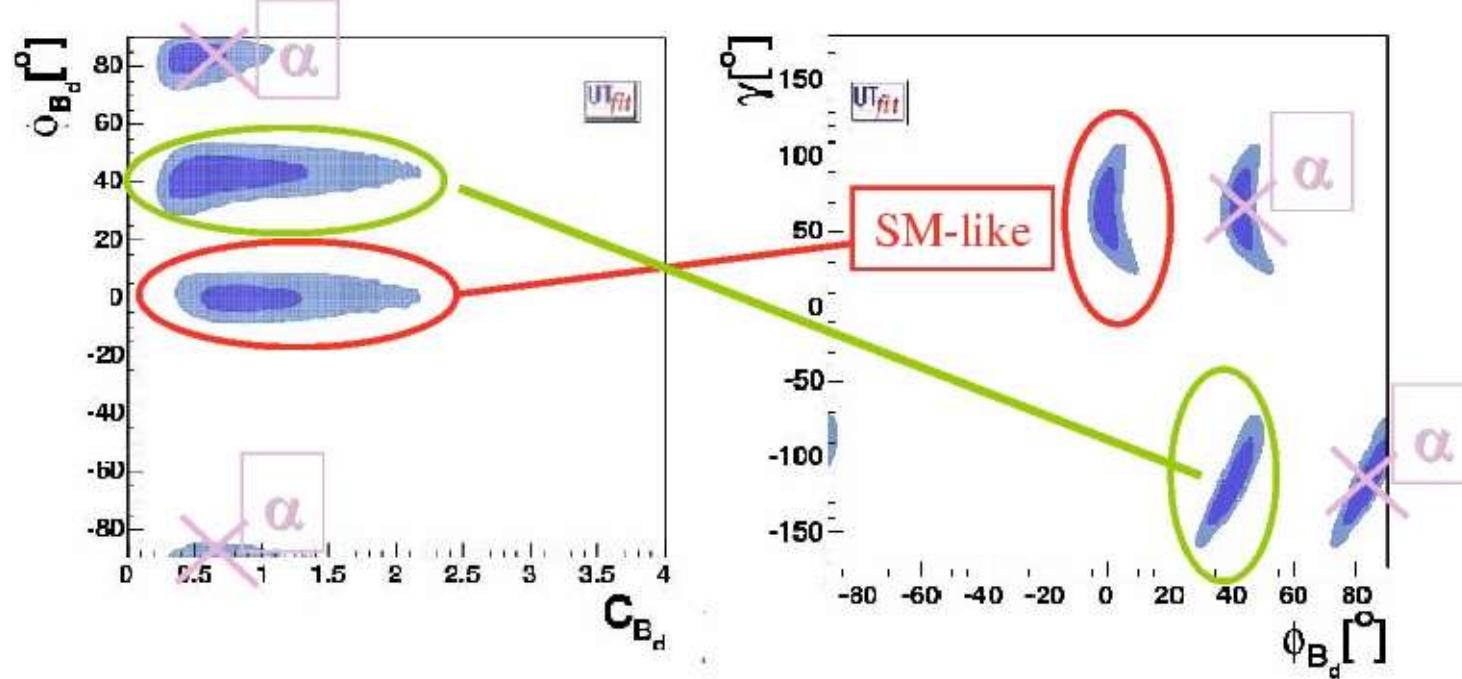


# Tree level+sides(fixing C's) and $\sin 2\beta$

**Using**

$|V_{ub}/V_{cb}|$   
 $\Delta m_d$   
 $\epsilon_K$   
 $A_{CP}(J/\psi K^0)$   
 $\gamma(DK)$

	$\gamma$	$C_d$	$\cos 2(\beta + \phi)$	$\sin 2(\alpha - \phi)$	$\sin(2\beta + \phi)$	$A_{SL}$
SM-LIKE	$60^\circ$	1	0.68	-0.23	0.96	OK
NP1	$60^\circ$	1	-0.68	0.96	-0.23	OK
NP2	$-120^\circ$	0.4	0.68	-0.23	-0.96	$10^{-2}$
NP3	$-120^\circ$	0.4	-0.68	0.96	0.23	OK

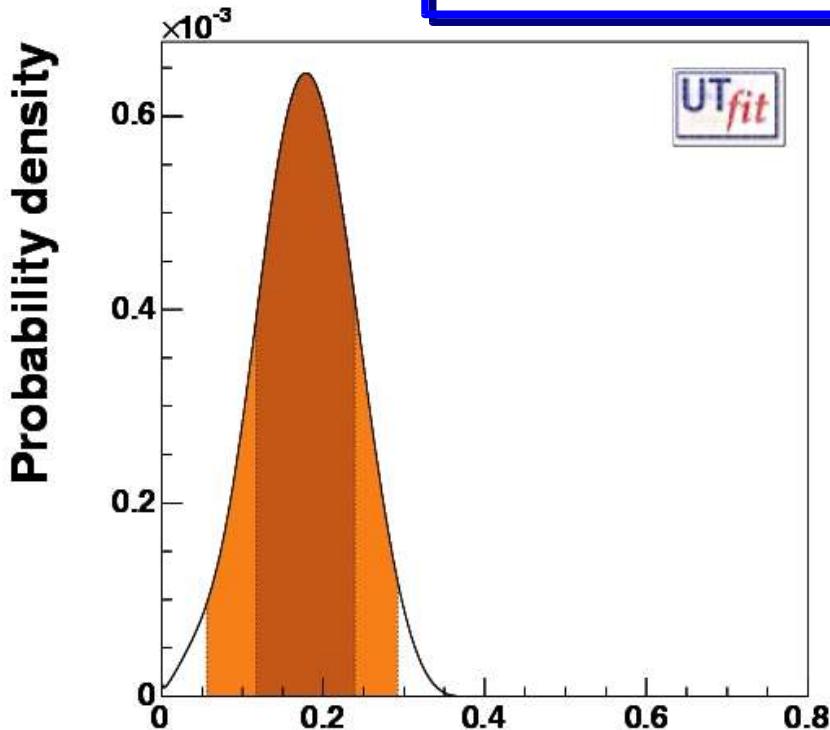




$B \rightarrow \tau\nu$

$$\mathcal{B}(B \rightarrow \ell\nu) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

$< 1.8 \cdot 10^{-4}$  @ 90% CL

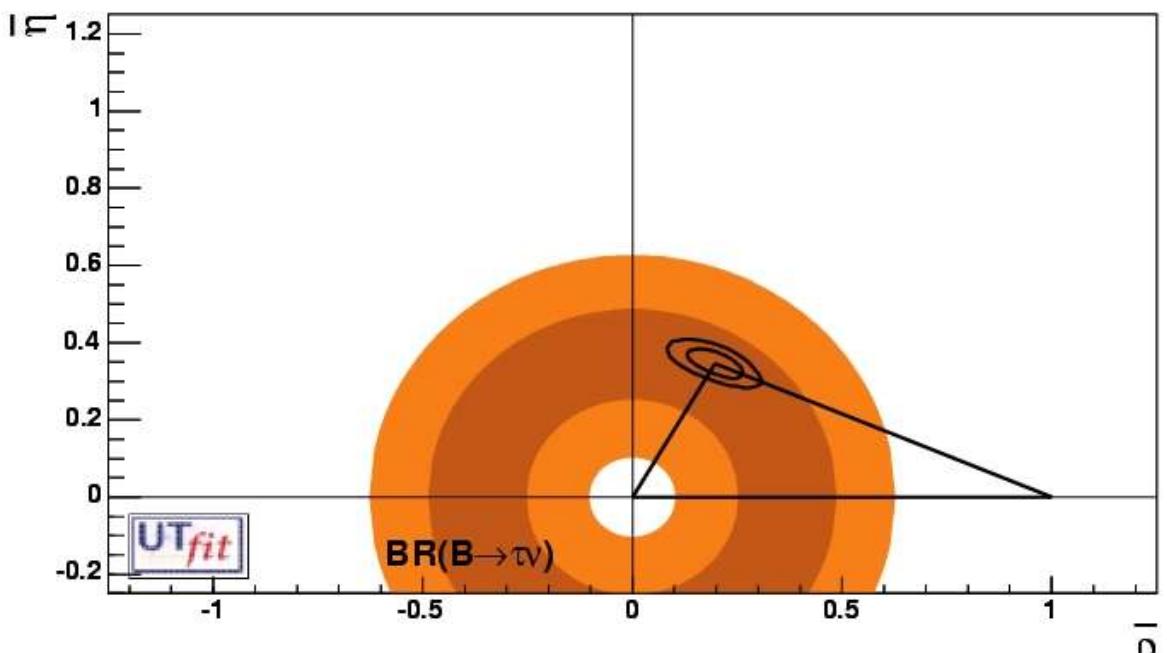


$f_{Bd} = 0.178 \pm 0.062 \text{ GeV}$

$f_{Bd} = 0.192 \pm 0.026 \pm 0.009 \text{ GeV}$

from lattice QCD

Assuming  $f_B$ :  
Constraint on  $R_b = \bar{\rho}^2 + \bar{\eta}^2$   
 $R_b = 0.37 \pm 0.13$





$$\text{BR}(\text{B} \rightarrow \rho\gamma) / \text{BR}(\text{B} \rightarrow K^*\gamma)$$

$$R = c_\rho^2 \frac{r_m}{\xi^2} \frac{|a_7^c(\rho\gamma)|^2}{|a_7^c(K^*\gamma)|^2} \frac{|V_{td}|^2}{|V_{ts}|^2} (1 + \Delta R)$$

In case of penguin dominance,  $R = \text{BR}(\text{B} \rightarrow \rho/\omega\gamma)/\text{BR}(\text{B} \rightarrow K^*\gamma)$   
can be used to extract  $|V_{td}/V_{ts}|$ , adding information wrt  $\Delta m_d/\Delta m_s$ .

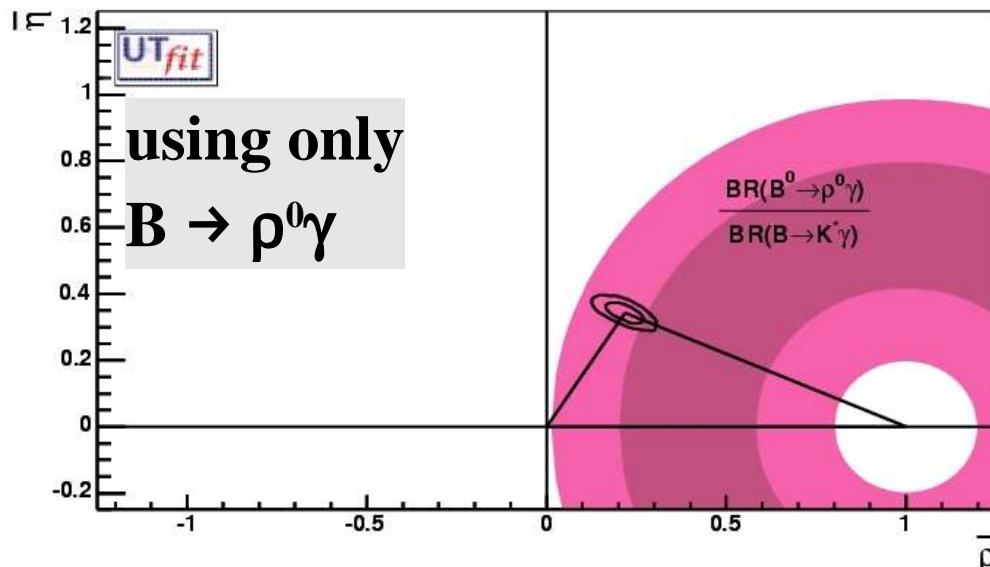
*caveat:* \* SU(3) breaking effect

$$\Delta R \sim \mathcal{O}(\Lambda_{\text{QCD}}/m_b)$$

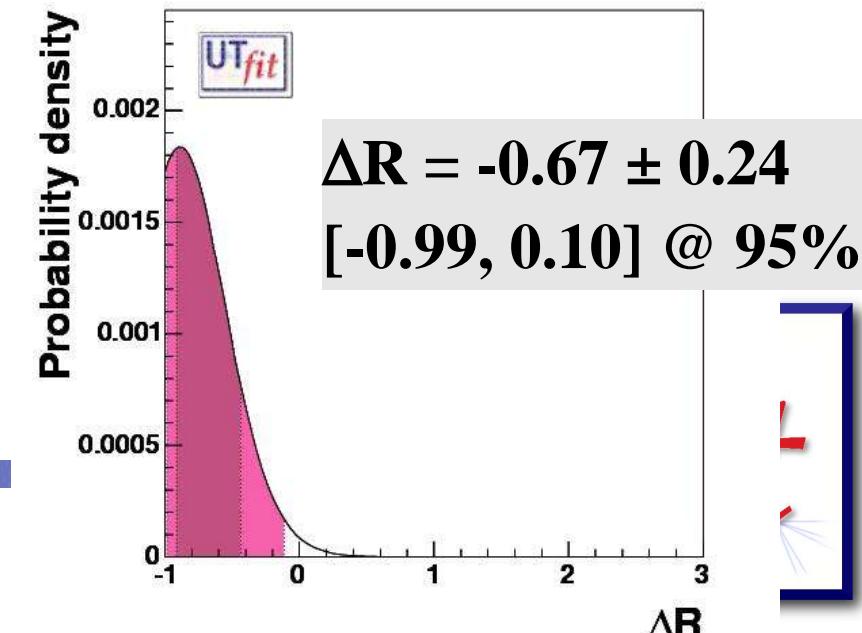
\* annihilation in  $\text{B}$  to  $\rho/\omega\gamma$  not in  $\text{B}$  to  $K^*\gamma$   
associated to a different CKM factor ( $\sim V_{ub}^* V_{ud}$ )

## QCD factorisation

$$|V_{td}/V_{ts}| = 0.10 \pm 0.45 \\ [0.02, 0.18] @ 95\% \text{ Prob.}$$



Using the  $|V_{td}/V_{ts}|$  value from the SM, we can extract  $\Delta R$ .





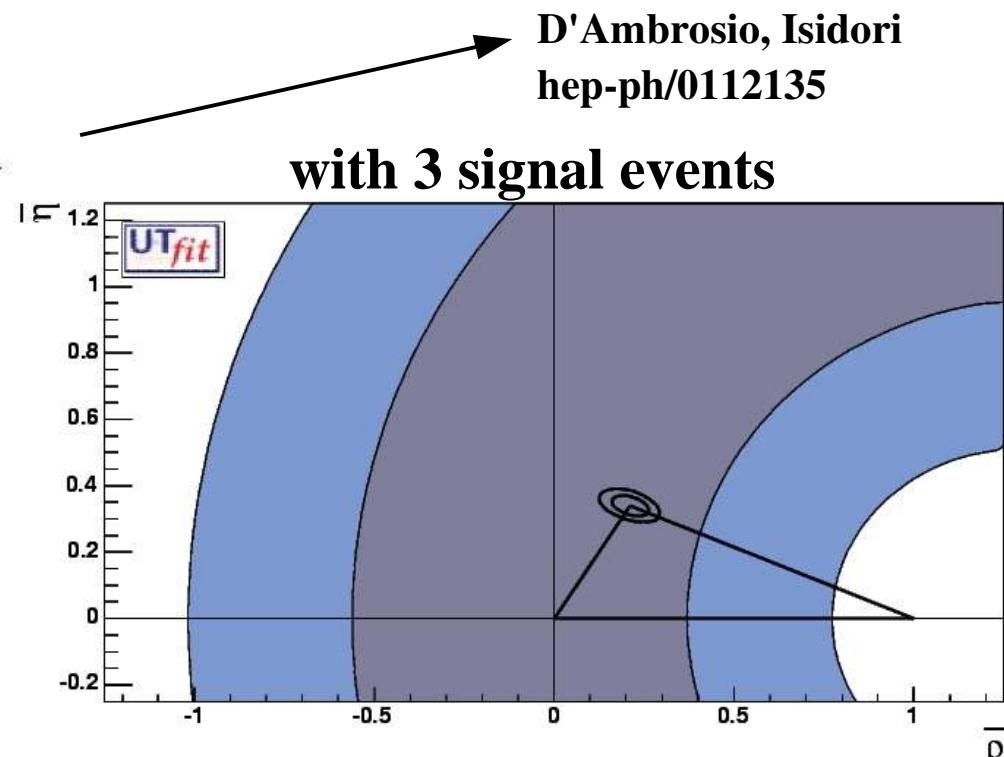
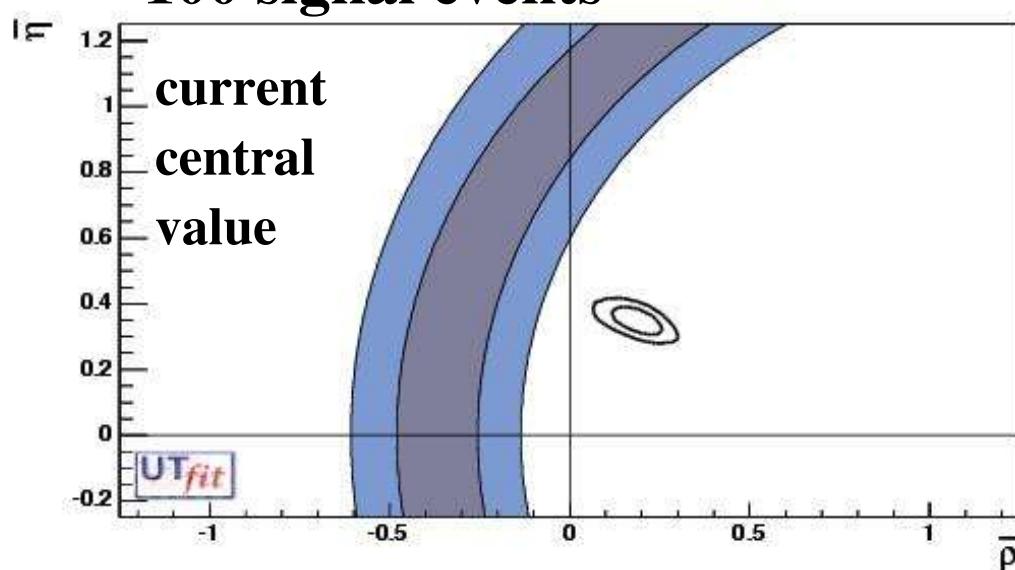
$$\underbrace{(\sigma\bar{\eta})^2 + (\bar{\rho} - \bar{\rho}_0)^2}_{\text{ellipse centered in } (\bar{\rho}^0, 0)} = \frac{\sigma BR(K^+ \rightarrow \pi^+ \nu\bar{\nu})}{\bar{\kappa}_+ |V_{cb}|^4 X^2(x_t)}$$

ellipse centered in  $(\bar{\rho}^0, 0)$

latest result from E949:

$$BR(K^\pm \rightarrow \pi^\pm \nu\bar{\nu}) = 1.47^{+1.30}_{-0.89} 10^{-10}$$

with the hypothesis of  
~100 signal events



using the value  
from the UTfit  
 $BR = 0.83 10^{-10}$

